

双曲三角函数及反双曲三角函数求导公式

$\sinh x = \frac{e^x - e^{-x}}{2}$	$(\sinh x)' = \cosh x = \frac{e^x + e^{-x}}{2}$
$\cosh x = \frac{e^x + e^{-x}}{2}$	$(\cosh x)' = \sinh x = \frac{e^x - e^{-x}}{2}$
$\tanh x = \frac{\sinh x}{\cosh x}$	$(\tanh x)' = \operatorname{sech}^2(x)$
$\operatorname{coth} x = \frac{1}{\tanh x}$	$(\operatorname{coth} x)' = -\operatorname{csch}^2 x$
$\operatorname{sech} x = \frac{1}{\cosh x}$	$(\operatorname{sech} x)' = -\tanh x \operatorname{sech} x$
$\operatorname{csch} x = \frac{1}{\sinh x}$	$(\operatorname{csch} x)' = -\operatorname{coth} x \operatorname{csch} x$
$\operatorname{arcsinh} x = \ln(x + \sqrt{x^2 + 1})$ $x \in (-\infty, +\infty)$	$(\operatorname{arcsinh} x)' = \frac{1}{\sqrt{x^2 + 1}}$
$\operatorname{arcosh} x = \ln(x + \sqrt{x^2 - 1})$ $x \in [1, +\infty)$	$(\operatorname{arcosh} x)' = \frac{1}{\sqrt{x^2 - 1}}$
$\operatorname{arctanh} x = \ln \sqrt{\frac{1+x}{1-x}}$ $(-1, 1)$	$(\operatorname{arctanh} x)' = \frac{1}{1-x^2}$
$\operatorname{arcsech} x = \pm \ln \frac{1 + \sqrt{1-x^2}}{x}$	$(\operatorname{arcsech} x)' = \frac{-1}{x\sqrt{1-x^2}}$
$\operatorname{csch}^{-1} x = \begin{cases} \ln \frac{1-\sqrt{1+x^2}}{x} & x < 0 \\ \ln \frac{1+\sqrt{1+x^2}}{x} & x > 0 \end{cases}$	$(\operatorname{arccsch} x)' = \frac{-1}{ x \sqrt{1-x^2}}$
$\operatorname{arccoth} x = \ln \sqrt{\frac{x+1}{x-1}}$ $x \in (-\infty, -1) \cup (1, +\infty)$	$(\operatorname{arccoth} x)' = \frac{1}{1-x^2}$